

MATHEMATICS · JEE MAIN

Straight Lines

Chapter-wise previous year questions, with answer key

39

PYQS

2020–2025

PAPERS

5

TOPICS

Distance from a Point to a Line

Locus

Distance and Section Formula

Forms of a Line

Angle Between Lines

- 1 Attempt each question on paper first. They're grouped by topic, newest papers first.
- 2 Check yourself against the answer key at the end.
- 3 Got one wrong? Tap “Step-by-step solution” under it for the full working.

Stuck on a question?

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Distance from a Point to a Line · 10 PYQs

Q1 JEE Main 2025 · 3 Apr · Shift 2

Let the equation $x(x+2)(12-k) = 2$ have equal roots. Then the distance of the point $(k, \frac{k}{2})$ from the line $3x + 4y + 5 = 0$ is

- (A) 15 (B) 12
(C) $5\sqrt{3}$ (D) $15\sqrt{5}$

Step-by-step solution ► [prepwiser.in/questions/BBaCGPCL-X](https://www.prepwiser.in/questions/BBaCGPCL-X)

Q2 JEE Main 2025 · 28 Jan · Shift 1

If $\alpha = 1 + \sum_{r=1}^6 (-3)^{r-1} {}^{12}C_{2r-1}$, then the distance of the point $(12, \sqrt{3})$ from the line $\alpha x - \sqrt{3}y + 1 = 0$ is _____.

Numerical answer: enter the value.

Step-by-step solution ► [prepwiser.in/questions/IMUj8WCGJA](https://www.prepwiser.in/questions/IMUj8WCGJA)

Q3 JEE Main 2024 · 8 Apr · Shift 2

If the image of the point $(-4, 5)$ in the line $x + 2y = 2$ lies on the circle $(x+4)^2 + (y-3)^2 = r^2$, then r is equal to:

- (A) 2 (B) 3
(C) 4 (D) 1

Step-by-step solution ► [prepwiser.in/questions/_BLa-gJ_m5](https://www.prepwiser.in/questions/_BLa-gJ_m5)

Q4 JEE Main 2024 · 30 Jan · Shift 2

If $x^2 - y^2 + 2hxy + 2gx + 2fy + c = 0$ is the locus of a point, which moves such that it is always equidistant from the lines $x + 2y + 7 = 0$ and $2x - y + 8 = 0$, then the value of $g + c + h - f$ equals

- (A) 8 (B) 14
(C) 29 (D) 6

Step-by-step solution ► [prepwiser.in/questions/ODBq-hJTjG](https://www.prepwiser.in/questions/ODBq-hJTjG)

Q5 JEE Main 2024 · 29 Jan · Shift 2

Let A be the point of intersection of the lines $3x + 2y = 14$, $5x - y = 6$ and B be the point of intersection of the lines $4x + 3y = 8$, $6x + y = 5$. The distance of the point $P(5, -2)$ from the line AB is

- (A) $\frac{13}{2}$ (B) 8
(C) $\frac{5}{2}$ (D) 6

Step-by-step solution ► [prepwiser.in/questions/_HWRhuE5Cs](https://www.prepwiser.in/questions/_HWRhuE5Cs)

Q6 JEE Main 2024 · 27 Jan · Shift 2

If the sum of squares of all real values of α , for which the lines $2x - y + 3 = 0$, $6x + 3y + 1 = 0$ and $\alpha x + 2y - 2 = 0$ do not form a triangle is p , then the greatest integer less than or equal to p is _____.

Numerical answer: enter the value.

Step-by-step solution ► [prepwiser.in/questions/2sAB0nJ8qk](https://www.prepwiser.in/questions/2sAB0nJ8qk)

Q7 JEE Main 2021 · 31 Aug · Shift 1

If p and q are the lengths of the perpendiculars from the origin on the lines,

$$x \operatorname{cosec} \alpha - y \sec \alpha = k \cot 2\alpha \text{ and}$$

$$x \sin \alpha + y \cos \alpha = k \sin 2\alpha$$

respectively, then k^2 is equal to :

(A) $4p^2 + q^2$

(B) $2p^2 + q^2$

(C) $p^2 + 2q^2$

(D) $p^2 + 4q^2$

[Step-by-step solution ► prepwiser.in/questions/0SpynPLfKB](https://www.prepwiser.in/questions/0SpynPLfKB)

Q8 JEE Main 2020 · 5 Sep · Shift 1

If the line, $2x - y + 3 = 0$ is at a distance

$\frac{1}{\sqrt{5}}$ and $\frac{2}{\sqrt{5}}$ from the lines $4x - 2y + \alpha = 0$

and $6x - 3y + \beta = 0$, respectively, then the sum of all possible values of α and β is :

Numerical answer: enter the value.

[Step-by-step solution ► prepwiser.in/questions/kOxrKsjvYg](https://www.prepwiser.in/questions/kOxrKsjvYg)

Q9 JEE Main 2020 · 4 Sep · Shift 2

Let PQ be a diameter of the circle $x^2 + y^2 = 9$. If α and β are the lengths of the perpendiculars from P and Q on the straight line,

$x + y = 2$ respectively, then the maximum value of $\alpha\beta$ is ____.

Numerical answer: enter the value.

[Step-by-step solution ► prepwiser.in/questions/1rGNKwzdLf](https://www.prepwiser.in/questions/1rGNKwzdLf)

Q10 JEE Main 2020 · 8 Jan · Shift 2

The length of the perpendicular from the origin, on the normal to the curve,

$x^2 + 2xy - 3y^2 = 0$ at the point $(2, 2)$ is

(A) $\sqrt{2}$

(B) $4\sqrt{2}$

(C) 2

(D) $2\sqrt{2}$

[Step-by-step solution ► prepwiser.in/questions/x6MUbn4ojT](https://www.prepwiser.in/questions/x6MUbn4ojT)

Q11 JEE Main 2025 · 28 Jan · Shift 2

If A and B are the points of intersection of the circle $x^2 + y^2 - 8x = 0$ and the hyperbola $\frac{x^2}{9} - \frac{y^2}{4} = 1$ and a point P moves on the line $2x - 3y + 4 = 0$, then the centroid of $\triangle PAB$ lies on the line :

- (A) $x + 9y = 36$
(B) $9x - 9y = 32$
(C) $4x - 9y = 12$
(D) $6x - 9y = 20$

[Step-by-step solution ► prepwisar.in/questions/fv4ho7MV7d](https://www.prepwisar.in/questions/fv4ho7MV7d)**Q12** JEE Main 2022 · 26 Jul · Shift 1

A point P moves so that the sum of squares of its distances from the points (1, 2) and (-2, 1) is 14. Let $f(x, y) = 0$ be the locus of P, which intersects the x -axis at the points A, B and the y -axis at the points C, D. Then the area of the quadrilateral ACBD is equal to :

- (A) $\frac{9}{2}$ (B) $\frac{3\sqrt{17}}{2}$
(C) $\frac{3\sqrt{17}}{4}$ (D) 9

[Step-by-step solution ► prepwisar.in/questions/MxzdjMBr_b](https://www.prepwisar.in/questions/MxzdjMBr_b)**Q13** JEE Main 2022 · 25 Jun · Shift 2

A circle touches both the y -axis and the line $x + y = 0$. Then the locus of its center is :

- (A) $y = \sqrt{2}x$ (B) $x = \sqrt{2}y$
(C) $y^2 - x^2 = 2xy$ (D) $x^2 - y^2 = 2xy$

[Step-by-step solution ► prepwisar.in/questions/W0wGHYZWYw](https://www.prepwisar.in/questions/W0wGHYZWYw)**Q14** JEE Main 2021 · 26 Aug · Shift 1

The locus of a point, which moves such that the sum of squares of its distances from the points (0, 0), (1, 0), (0, 1), (1, 1) is 18 units, is a circle of diameter d. Then d^2 is equal to _____.

Numerical answer: enter the value.

[Step-by-step solution ► prepwisar.in/questions/sTLOcaG3NJ](https://www.prepwisar.in/questions/sTLOcaG3NJ)**Q15** JEE Main 2021 · 24 Feb · Shift 2

Let a point P be such that its distance from the point (5, 0) is thrice the distance of P from the point (-5, 0). If the locus of the point P is a circle of radius r, then $4r^2$ is equal to _____

Numerical answer: enter the value.

[Step-by-step solution ► prepwisar.in/questions/1WWv_MLmoj](https://www.prepwisar.in/questions/1WWv_MLmoj)

Distance and Section Formula · 13 PYQs

Q16 JEE Main 2025 · 7 Apr · Shift 1

Let ABC be the triangle such that the equations of lines AB and AC be $3y - x = 2$ and $x + y = 2$, respectively, and the points B and C lie on x -axis. If P is the orthocentre of the triangle ABC, then the area of the triangle PBC is equal to

- (A) 8 (B) 4
(C) 10 (D) 6

Step-by-step solution ► [prepwisser.in/questions/u7X_JDgR5m](https://www.prepwisser.in/questions/u7X_JDgR5m)

Q17 JEE Main 2025 · 22 Jan · Shift 2

Let the distance between two parallel lines be 5 units and a point P lie between the lines at a unit distance from one of them. An equilateral triangle PQR is formed such that Q lies on one of the parallel lines, while R lies on the other. Then $(QR)^2$ is equal to _____.

Numerical answer: enter the value.

Step-by-step solution ► [prepwisser.in/questions/vUV3aV06RA](https://www.prepwisser.in/questions/vUV3aV06RA)

Q18 JEE Main 2025 · 22 Jan · Shift 1

Let the triangle PQR be the image of the triangle with vertices $(1, 3)$, $(3, 1)$ and $(2, 4)$ in the line $x + 2y = 2$. If the centroid of $\triangle PQR$ is the point (α, β) , then $15(\alpha - \beta)$ is equal to :

- (A) 21 (B) 19
(C) 22 (D) 24

Step-by-step solution ► [prepwisser.in/questions/rzuBaAcEcQ](https://www.prepwisser.in/questions/rzuBaAcEcQ)

Q19 JEE Main 2023 · 13 Apr · Shift 2

Let (α, β) be the centroid of the triangle formed by the lines $15x - y = 82$, $6x - 5y = -4$ and $9x + 4y = 17$. Then $\alpha + 2\beta$ and $2\alpha - \beta$ are the roots of the equation :

- (A) $x^2 - 7x + 12 = 0$ (B) $x^2 - 13x + 42 = 0$
(C) $x^2 - 14x + 48 = 0$ (D) $x^2 - 10x + 25 = 0$

Step-by-step solution ► [prepwisser.in/questions/TDhcdEcxkm](https://www.prepwisser.in/questions/TDhcdEcxkm)

Q20 JEE Main 2023 · 29 Jan · Shift 1

Let B and C be the two points on the line $y + x = 0$ such that B and C are symmetric with respect to the origin. Suppose A is a point on $y - 2x = 2$ such that $\triangle ABC$ is an equilateral triangle. Then, the area of the $\triangle ABC$ is :

- (A) $\frac{10}{\sqrt{3}}$ (B) $2\sqrt{3}$
(C) $3\sqrt{3}$ (D) $\frac{8}{\sqrt{3}}$

Step-by-step solution ► [prepwisser.in/questions/v_lxiDvqC](https://www.prepwisser.in/questions/v_lxiDvqC)

Q21 JEE Main 2022 · 29 Jun · Shift 1

The distance between the two points A and A' which lie on $y = 2$ such that both the line segments AB and A'B (where B is the point (2, 3)) subtend angle $\frac{\pi}{4}$ at the origin, is equal to :

- (A) 10 (B) $\frac{48}{5}$
(C) $\frac{52}{5}$ (D) 3

Step-by-step solution ► [prepwiser.in/questions/IFcyJo-z6Z](https://www.prepwiser.in/questions/IFcyJo-z6Z)

Q22 JEE Main 2022 · 24 Jun · Shift 2

Let the area of the triangle with vertices A(1, α), B(α , 0) and C(0, α) be 4 sq. units. If the points (α , $-\alpha$), ($-\alpha$, α) and (α^2 , β) are collinear, then β is equal to :

- (A) 64 (B) -8
(C) -64 (D) 512

Step-by-step solution ► [prepwiser.in/questions/33uaHwWw7L](https://www.prepwiser.in/questions/33uaHwWw7L)

Q23 JEE Main 2022 · 24 Jun · Shift 1

Let $A\left(\frac{3}{\sqrt{a}}, \sqrt{a}\right)$, $a > 0$, be a fixed point in the xy-plane. The image of A in y-axis be B and the image of B in x-axis be C. If $D(3 \cos \theta, a \sin \theta)$ is a point in the fourth quadrant such that the maximum area of $\triangle ACD$ is 12 square units, then a is equal to _____.

Numerical answer: enter the value.

Step-by-step solution ► [prepwiser.in/questions/Wj5oF6KGq5](https://www.prepwiser.in/questions/Wj5oF6KGq5)

Q24 JEE Main 2021 · 27 Aug · Shift 2

Let A(a, 0), B(b, 2b + 1) and C(0, b), $b \neq 0$, $|b| \neq 1$, be points such that the area of triangle ABC is 1 sq. unit, then the sum of all possible values of a is :

- (A) $\frac{-2b}{b+1}$ (B) $\frac{2b}{b+1}$
(C) $\frac{2b^2}{b+1}$ (D) $\frac{-2b^2}{b+1}$

Step-by-step solution ► [prepwiser.in/questions/B3Ie_g8_Kv](https://www.prepwiser.in/questions/B3Ie_g8_Kv)

Q25 JEE Main 2021 · 17 Mar · Shift 1

In a triangle PQR, the co-ordinates of the points P and Q are (-2, 4) and (4, -2) respectively. If the equation of the perpendicular bisector of PR is $2x - y + 2 = 0$, then the centre of the circumcircle of the $\triangle PQR$ is :

- (A) (-1, 0) (B) (1, 4)
(C) (0, 2) (D) (-2, -2)

Step-by-step solution ► [prepwiser.in/questions/tBStH81732](https://www.prepwiser.in/questions/tBStH81732)

Q26 JEE Main 2021 · 17 Mar · Shift 2

Let $\tan \alpha$, $\tan \beta$ and $\tan \gamma$; $\alpha, \beta, \gamma \neq \frac{(2n-1)\pi}{2}$, $n \in \mathbb{N}$ be the slopes of three line segments OA, OB and OC, respectively, where O is origin. If circumcentre of $\triangle ABC$ coincides with origin and its orthocentre lies on y-axis, then the value of $\left(\frac{\cos 3\alpha + \cos 3\beta + \cos 3\gamma}{\cos \alpha \cos \beta \cos \gamma}\right)^2$ is equal to _____.

Numerical answer: enter the value.

Step-by-step solution ► [prepwiser.in/questions/nxNeTrc7im](https://www.prepwiser.in/questions/nxNeTrc7im)

Q27 JEE Main 2020 · 9 Jan · Shift 1

Let C be the centroid of the triangle with vertices (3, -1), (1, 3) and (2, 4). Let P be the point of intersection of the lines $x + 3y - 1 = 0$ and $3x - y + 1 = 0$. Then the line passing through the points C and P also passes through the point :

(A) (-9, -7)

(B) (9, 7)

(C) (7, 6)

(D) (-9, -6)

[Step-by-step solution ► prepwisser.in/questions/Yzhs4tScYM](https://www.prepwisser.in/questions/Yzhs4tScYM)

Q28 JEE Main 2020 · 8 Jan · Shift 1

Let two points be A(1, -1) and B(0, 2). If a point P(x', y') be such that the area of $\triangle PAB = 5$ sq. units and it lies on the line, $3x + y - 4\lambda = 0$, then a value of λ is :

(A) 4

(B) 1

(C) -3

(D) 3

[Step-by-step solution ► prepwisser.in/questions/sX4GkYA10-](https://www.prepwisser.in/questions/sX4GkYA10-)

Forms of a Line · 9 PYQs

Q29 JEE Main 2024 · 1 Feb · Shift 2

The lines $L_1, L_2, \dots, L_{20}$ are distinct. For $n = 1, 2, 3, \dots, 10$ all the lines L_{2n-1} are parallel to each other and all the lines L_{2n} pass through a given point P. The maximum number of points of intersection of pairs of lines from the set $\{L_1, L_2, \dots, L_{20}\}$ is equal to _____.

Numerical answer: enter the value.

[Step-by-step solution ► prepwisser.in/questions/kUZzg731qb](https://www.prepwisser.in/questions/kUZzg731qb)

Q30 JEE Main 2022 · 29 Jul · Shift 2

Let m_1, m_2 be the slopes of two adjacent sides of a square of side a such that $a^2 + 11a + 3(m_1^2 + m_2^2) = 220$. If one vertex of the square is $(10(\cos \alpha - \sin \alpha), 10(\sin \alpha + \cos \alpha))$, where $\alpha \in (0, \frac{\pi}{2})$ and the equation of one diagonal is $(\cos \alpha - \sin \alpha)x + (\sin \alpha + \cos \alpha)y = 10$, then $72(\sin^4 \alpha + \cos^4 \alpha) + a^2 - 3a + 13$ is equal to :

(A) 119

(B) 128

(C) 145

(D) 155

[Step-by-step solution ► prepwisser.in/questions/KtZ-0zmROg](https://www.prepwisser.in/questions/KtZ-0zmROg)

Q31 JEE Main 2021 · 27 Jul · Shift 2

The point P (a, b) undergoes the following three transformations successively :

- (a) reflection about the line $y = x$.
- (b) translation through 2 units along the positive direction of x-axis.
- (c) rotation through angle $\frac{\pi}{4}$ about the origin in the anti-clockwise direction.

If the co-ordinates of the final position of the point P are $\left(-\frac{1}{\sqrt{2}}, \frac{7}{\sqrt{2}}\right)$, then the value of $2a + b$ is equal to :

- (A) 13
- (B) 9
- (C) 5
- (D) 7

[Step-by-step solution ► prepwiser.in/questions/wfjnnqOE5y](https://www.prepwiser.in/questions/wfjnnqOE5y)

Q32 JEE Main 2021 · 18 Mar · Shift 1

The number of integral values of m so that the abscissa of point of intersection of lines $3x + 4y = 9$ and $y = mx + 1$ is also an integer, is :

- (A) 1
- (B) 2
- (C) 3
- (D) 0

[Step-by-step solution ► prepwiser.in/questions/U9JRXsw5VN](https://www.prepwiser.in/questions/U9JRXsw5VN)

Q33 JEE Main 2021 · 26 Feb · Shift 1

The intersection of three lines $x - y = 0$, $x + 2y = 3$ and $2x + y = 6$ is a :

- (A) Right angled triangle
- (B) Equilateral triangle
- (C) None of the above
- (D) Isosceles triangle

[Step-by-step solution ► prepwiser.in/questions/rC7x5GNSZZ](https://www.prepwiser.in/questions/rC7x5GNSZZ)

Q34 JEE Main 2021 · 25 Feb · Shift 1

The image of the point (3, 5) in the line $x - y + 1 = 0$, lies on :

- (A) $(x - 4)^2 + (y - 4)^2 = 8$
- (B) $(x - 4)^2 + (y + 2)^2 = 16$
- (C) $(x - 2)^2 + (y - 2)^2 = 12$
- (D) $(x - 2)^2 + (y - 4)^2 = 4$

[Step-by-step solution ► prepwiser.in/questions/kqAYv6dOKX](https://www.prepwiser.in/questions/kqAYv6dOKX)

Q35 JEE Main 2020 · 6 Sep · Shift 2

Let L denote the line in the xy-plane with x and y intercepts as 3 and 1 respectively. Then the image of the point (-1, -4) in this line is :

- (A) $\left(\frac{11}{5}, \frac{28}{5}\right)$
- (B) $\left(\frac{29}{5}, \frac{11}{5}\right)$
- (C) $\left(\frac{29}{5}, \frac{8}{5}\right)$
- (D) $\left(\frac{8}{5}, \frac{29}{5}\right)$

[Step-by-step solution ► prepwiser.in/questions/O24t4SRNdG](https://www.prepwiser.in/questions/O24t4SRNdG)

Q36 JEE Main 2020 · 4 Sep · Shift 2

If the perpendicular bisector of the line segment joining the points $P(1, 4)$ and $Q(k, 3)$ has y-intercept equal to -4 , then a value of k is :

- (A) $\sqrt{14}$ (B) -4
(C) -2 (D) $\sqrt{15}$

Step-by-step solution ► [prepwisser.in/questions/NY0w-AKAgs](https://www.prepwisser.in/questions/NY0w-AKAgs)

Q37 JEE Main 2020 · 2 Sep · Shift 2

The set of all possible values of θ in the interval $(0, \pi)$ for which the points $(1, 2)$ and $(\sin \theta, \cos \theta)$ lie on the same side of the line $x + y = 1$ is :

- (A) $(0, \frac{\pi}{4})$
(B) $(0, \frac{3\pi}{4})$
(C) $(\frac{\pi}{4}, \frac{3\pi}{4})$
(D) $(0, \frac{\pi}{2})$

Step-by-step solution ► [prepwisser.in/questions/QVCUA4sC5i](https://www.prepwisser.in/questions/QVCUA4sC5i)

Angle Between Lines · 2 PYQs

Q38 JEE Main 2024 · 8 Apr · Shift 2

If the line segment joining the points $(5, 2)$ and $(2, a)$ subtends an angle $\frac{\pi}{4}$ at the origin, then the absolute value of the product of all possible values of a is :

- (A) 4 (B) 8
(C) 6 (D) 2

Step-by-step solution ► [prepwisser.in/questions/TVkMx6XAg5](https://www.prepwisser.in/questions/TVkMx6XAg5)

Q39 JEE Main 2021 · 18 Mar · Shift 1

The equation of one of the straight lines which passes through the point $(1, 3)$ and makes an angle $\tan^{-1}(\sqrt{2})$ with the straight line, $y + 1 = 3\sqrt{2}x$ is :

- (A) $4\sqrt{2}x + 5y - (15 + 4\sqrt{2}) = 0$
(B) $5\sqrt{2}x + 4y - (15 + 4\sqrt{2}) = 0$
(C) $4\sqrt{2}x + 5y - 4\sqrt{2} = 0$
(D) $4\sqrt{2}x - 5y - (5 + 4\sqrt{2}) = 0$

Step-by-step solution ► [prepwisser.in/questions/EBWyxGH_4n](https://www.prepwisser.in/questions/EBWyxGH_4n)

Answer key: Straight Lines

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9	7	10	D	11	D	12	B	13	D	14	16	15	56	16	D
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